

# VU Programm- und Systemverifikation

## Homework: Hoare Logic

May 27, 2015

**Task 1 (8 points):** Prove the Hoare Triple below (assume that the domain of all variables in the program are the natural numbers including 0). You need to find a sufficiently strong loop invariant. Annotate the following code directly with the required assertions. Justify each assertion by stating which Hoare rule you used to derive it.

```
{true}
```

```
if (x > y) {
```

```
    a = x;
```

```
    b = y;
```

```
} else {
```

```
    a = y;
```

```
    b = x;
```

```
}
```

```
while ((a-b)>0) {
```

```
    a = a-1;
```

```
}
```

```
{a = b}
```

**Task 2 (7 points):** Prove the Hoare Triple below (assume that the domain of all variables in the program are the integers, and that  $N$  is a positive constant). You need to find a sufficiently strong loop invariant. Annotate the following code directly with the required assertions. Justify each assertion by stating which Hoare rule you used to derive it.

{true}

$x := N;$

$y := 0;$

while ( $x > 0$ ) {

$x = x - 1;$

$y = y + 1;$

}

{ $y = N$ }

Upload a pdf file with your solutions to TUWEL by June 10, 2015.